



Affine invariant classification and retrieval of texture images [☆]

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Abstract

In this paper, we propose a new method of extracting affine invariant texture signatures for content-based affine invariant image retrieval (CBAIR). The algorithm discussed in this paper exploits the spectral signatures of texture images. Based on spectral representation of affine transform, anisotropic scale invariant signatures of orientation spectrum distributions are extracted. Peaks distribution vector (PDV) obtained from signature distributions captures texture properties invariant to affine transform. The PDV is used to measure the similarity between textures. Extensive experimental results are included to demonstrate the performance of the method in texture classification and CBAIR.

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1. Introduction

Content-based image retrieval is a very active research topic in recent years. With the development of the Internet, the number of images that Internet users could access increases almost exponentially. Accordingly, powerful retrieval tools of Web images are highly desirable.

A great deal of work on image retrieval has been done during the past years. Comprehensive surveys of these methods may be found in Refs. [1–4]. The features commonly used for content-based image retrieval include color, texture, sketch, shape, etc. [1]. Texture features play a very important role in computer vision and pattern recognition, especially in describing the content of images. Images in a digital database are usually subject to geometric distortions

due to change of viewpoints. So the retrieval tools should ideally be invariant to such distortions. Invariant image descriptions deserve more attention [1,5,6], and a new challenge is content-based viewpoint invariant image retrieval. The majority of existing work on invariant texture description has been focused on obtaining translation and rotation invariance [7–10]. Texture descriptors found in the literature are hardly invariant to affine or perspective transform. Such higher-level invariance is however desirable in practical content-based image retrieval systems. This is a very difficult and challenging problem.

This paper attempts to tackle this hard problem by focusing on affine invariant texture feature extraction, and its application in CBAIR. The algorithm discussed in this paper exploits the spectral signatures of texture images. Based on the spectral representation of affine transform, anisotropic scale invariant signatures of orientation spectrum distribution are extracted. Peaks distribution vector (PDV) obtained from signature distributions captures texture properties invariant to affine transform. The PDV is used to measure the similarity between textures. Extensive experimental results are included to demonstrate the performance of the method in texture classification and CBAIR.

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2. Normalization of texture spectrum representation under affine transform

It is well known that affine transform can be decomposed into scale, skew, rotation and translation. It can be viewed as the approximation of the perspective projection if the depth of an object is relatively large with respect to its dimension [11].

Let $f(x, y)$ be the original image and $f_a(x_a, y_a)$ its affine transformed version. Then the relationship of these two images is as follows:

$$f_a(x_a, y_a) = f(x, y); \begin{bmatrix} x_a \\ y_a \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} \\ c_{21} & c_{22} \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} + \begin{bmatrix} d_1 \\ d_2 \end{bmatrix}. \tag{1}$$

Let matrix A denote

$$\begin{bmatrix} c_{11} & c_{12} \\ c_{21} & c_{22} \end{bmatrix} \quad \text{and} \quad D \begin{bmatrix} d_1 \\ d_2 \end{bmatrix}.$$

D is the translation factor and A is the rotation and scaling factor. It is easy to see that when the original texture undergoes an affine transform, its frequency spectrum undergoes a similar affine transform.

Let $F(u, v)$ be the Fourier transform of the original texture $f(x, y)$, $F_a(u_a, v_a)$ that of $f_a(x_a, y_a)$. Thus we can obtain the following equations (here we assume that $\det(A^{-1}) \neq 0$) [5]:

$$|F_a(u_a, v_a)| = \det(A^{-1})|F(u, v)|, \quad \begin{pmatrix} u_a \\ v_a \end{pmatrix} = A_T^{-1} \begin{pmatrix} u \\ v \end{pmatrix}, \tag{2}$$

where A_T^{-1} is the inverse of the transpose of matrix A .

From Eqs. (2) and (1), we can see that the two expressions are very similar except that the spectrum in Eq. (2) is scaled by $\det(A^{-1})$ and the translation factor D is removed. So that if Eq. (2) is normalized by the sum of $|F(u, v)|$, the following equation can be obtained:

$$\frac{|F_a(u_a, v_a)|}{\sum_{u_a, v_a=-\infty}^{+\infty} |F_a(u_a, v_a)|} = \frac{|F(u, v)|}{\sum_{u, v=-\infty}^{+\infty} |F(u, v)|}. \tag{3}$$

Let $F'_a(u_a, v_a)$ denote the left part of Eq. (3) and $F'(u, v)$ the right part. By rewriting Eq. (3), we get

$$|F'_a(u_a, v_a)| = |F'(u, v)|, \quad \begin{pmatrix} u_a \\ v_a \end{pmatrix} = A_T^{-1} \begin{pmatrix} u \\ v \end{pmatrix}. \tag{4}$$

Thus the normalized spectrum also satisfies the affine model. The relationship between textures and their spectral representations under affine transform is illustrated in Fig. 1.

3. Affine invariant texture signatures

In Section 2, we have shown that affine transform in the spatial domain results in similar affine transform in the

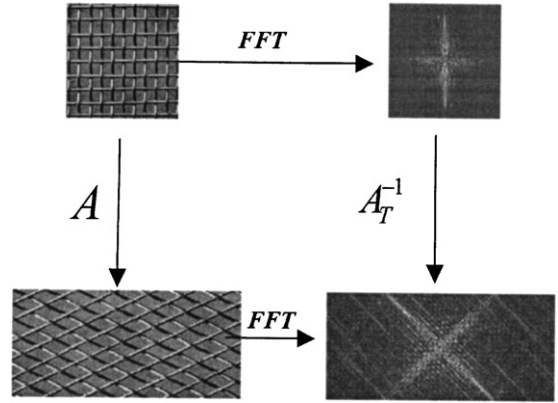


Fig. 1. Spectral representation of textures under affine transform.

spectrum. We have also derived a spectral representation (Eq. (4)) that mathematically satisfies affine model. This indicates that we can derive texture properties from its spectrum that are invariant to affine transforms (notice that spectrum contains most of the useful texture information of the original image). This section discusses whether and how we can use the new representation for affine invariant texture analysis.

In order to simplify notations, here we simply use $F_a(u_a, v_a)$ ($F(u, v)$) to represent $|F'_a(u_a, v_a)|$ ($|F'(u, v)|$), that is

$$F_a(u_a, v_a) = F(u, v); \quad \begin{pmatrix} u_a \\ v_a \end{pmatrix} = \hat{A} \begin{pmatrix} u \\ v \end{pmatrix}, \tag{5}$$

where \hat{A} denotes the matrix

$$A_T^{-1} = \begin{bmatrix} \hat{c}_{11} & \hat{c}_{12} \\ \hat{c}_{21} & \hat{c}_{22} \end{bmatrix}.$$

Let

$$\rho_a = \sqrt{u_a^2 + v_a^2}, \quad \theta_a = \text{arctg}(u_a/v_a),$$

$$\rho = \sqrt{u^2 + v^2}, \quad \theta = \text{arctg}(u/v).$$

Eq. (5) can then be expressed in its polar version

$$F_a(\rho_a, \theta_a) = F(\rho, \theta), \tag{6}$$

where $F_a(\rho_a, \theta_a)$ and $F(\rho, \theta)$ are called the line-spread functions [12] along the lines at angle θ_a and θ . We have investigated the changes between ρ and ρ_a in our previous work [13] by using their ratio s ($s = \rho_a/\rho$). Our study indicates that s is only dependent on θ for a given affine transform. Although s varies with θ , s is a fixed value for a given orientation θ . By applying log operation on ρ and ρ_a along the orientation θ and θ_a , we have

$$F_a(w_1, \theta_a) = F(w_2, \theta), \tag{7}$$

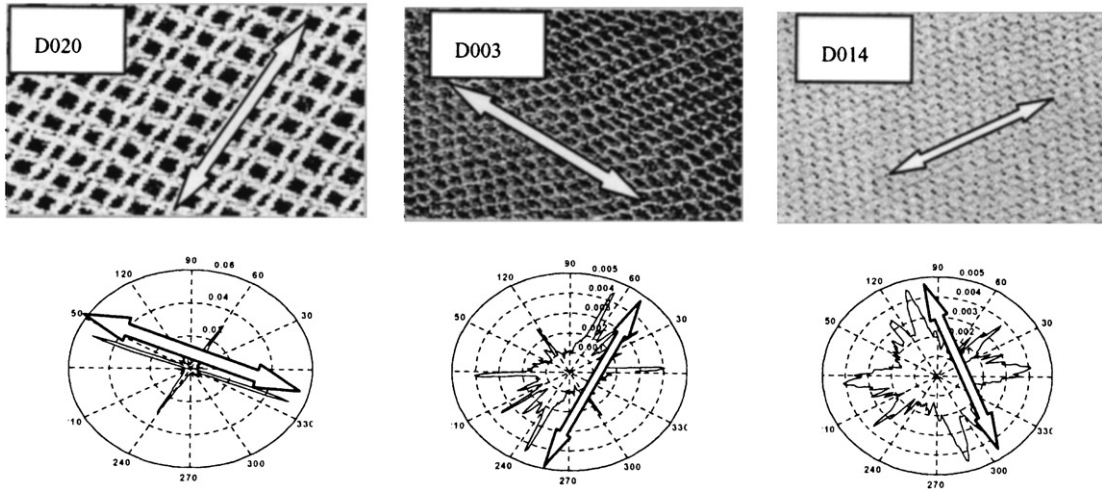


Fig. 2. Examples of spectrum signatures of different textures from the Brodatz album. Arrows show the main texture direction indicated by texture signatures.

where

$$w_1 = \log \rho_a = \log s + \log \rho,$$

$$w_2 = \log \rho.$$

It is important to note that in Eq. (7) scaling in the line-spread spectrum function has been transformed into a shift by the log operation. Since the frequency distribution (here we consider the spectrum magnitude as the probability of the corresponding frequency) can give a description of texture periodicity [14], we calculate the central moment of the line spread function as follows:

$$c_a(\theta_a) = \int_0^{+\infty} (w_1 - \bar{w}_1)^2 F_a(w_1, \theta_a) dw_1,$$

$$c(\theta) = \int_0^{+\infty} (w_2 - \bar{w}_2)^2 F(w_2, \theta) dw_2, \quad (8)$$

where \bar{w}_1 and \bar{w}_2 are the mean value of w_1 and w_2 along each orientation. They can be computed via the following equations:

$$\bar{w}_1 = \frac{\int_0^{+\infty} w_1 F_a(w_1, \theta_a) dw_1}{\int_0^{+\infty} F_a(w_1, \theta_a) dw_1},$$

$$\bar{w}_2 = \frac{\int_0^{+\infty} w_2 F(w_2, \theta) dw_1}{\int_0^{+\infty} F(w_2, \theta) dw_2}.$$

Since the shift factor has been removed in Eq. (8), it is obviously that $c_a(\theta_a)$ equals to $c(\theta)$. Notice that the power spectrum also plays a very important role in measuring texture properties. We incorporate the normalized power spectrum that is invariant to scaling and compute the

spectrum signatures at angle θ and θ_a as follows:

$$T(\theta_a) = c_a(\theta_a) \int_0^{+\infty} F_a(w_1, \theta_a) dw_1$$

$$= c(\theta) \int_0^{+\infty} F(w_2, \theta) dw_2 = T(\theta). \quad (9)$$

We have now obtained the orientation spectrum signature $T(\theta)$ which is invariant to anisotropic scale (notice that affine transform results in different scaling along different orientations. It is often overlooked in most of the literature on invariant texture analysis). This is the key problem of affine invariant texture analysis.

When we investigate the spectrum signatures along all the orientations throughout the whole image, $T(\theta)$ becomes the distribution function of spectrum signatures at different angles (here we call this function as signature distribution function). The major peaks of $T(\theta)$ indicate those specific, dominating directions within the spectrum domain, which in turn reflect strong texture directionality as illustrated in Fig. 2.

Fig. 3 gives an example of the effect of affine transform on texture signatures. From this figure, we can see that although the signature distribution function changes under affine transform, the order of the major peaks, the number of the peaks, and the magnitude of the peaks tend to be quite stable. That is the PDV almost remains the same. Similar observation can also be found in [15].

The PDV is constructed based on those peaks. A peak p_i of $T(\theta)$ is defined as follows:

$$p_i = T(\theta_i), \quad (10)$$

when $T(\theta_i)$ satisfies the following conditions:

$$1. \quad T(\theta_i) = \max_{m \in W_s} (T(\theta_m)), \quad m \in \left\{ i - \frac{W_s}{2}, i + \frac{W_s}{2} \right\}; \quad (11)$$

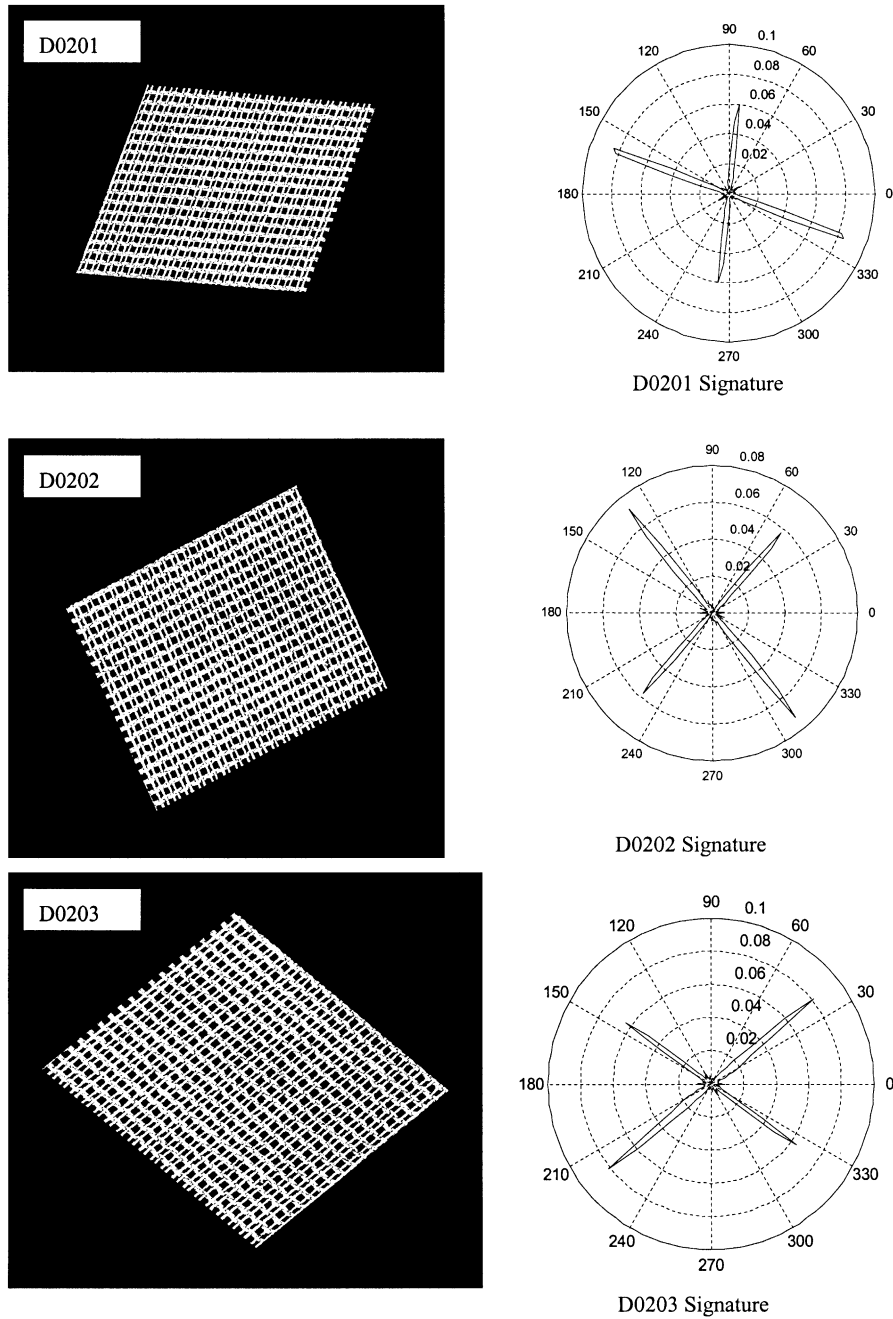


Fig. 3. Affine transformed versions of texture D020 and their corresponding signatures.

$$2. \int_m \left(T(\theta_m) - \frac{1}{w_s} \int_m T(\theta_m) d\theta \right)^2 d\theta \geq t, \quad (12)$$

where t is a given threshold to select the peaks and w_s is the size of the local window of θ_m . Since the spacing between peaks can be small, the size of the local window cannot be

very large. Here we use the local window size of 1×7 . Condition 1 (Eq. (11)) implies that the value of the central point of the peak support window must be a local maximum. Condition 2 (Eq. (12)) suggests that a local maximum qualifies for a peak only when the deviation of its adjacent area is no less than a given threshold. In fact it gives a measurement

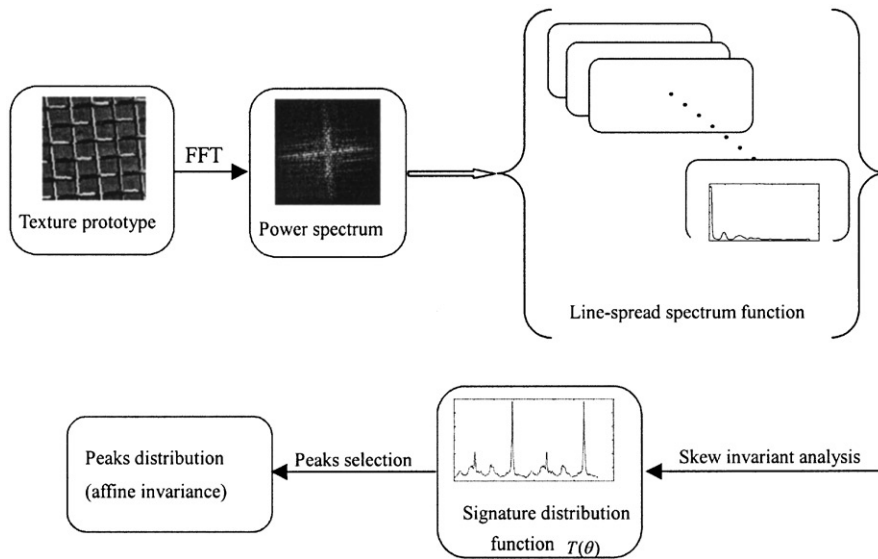


Fig. 4. Schematic diagram of PDV extraction.

of smoothness of the peak profile. Note that the noise of the signature must be first removed since it may affect peak detection. Here Gaussian filter is first applied to denoise the signature. The process of the PDV extraction is illustrated in Fig. 4.

The affine invariant feature vector is constructed by computing statistics of PDV. The statistics we used here are the largest value, the average value, the standard deviation, and the peak density. The peak density is calculated as the ratio between the number of peaks and the length of θ .

The following outlines the major steps of computing the affine invariant texture features:

1. Compute the Fourier transform of an original texture image, and then normalize its magnitude by its 1-norm as described in Eq. (3);
2. Extract the line-spread function along each orientation. This step needs to sample the magnitude domain along its orientation axis. Usually the sample interval is 1° ;
3. Apply the log operation on every line-spread function and compute $T(\theta)$ according to Eq. (9). Thus the signature distribution is obtained;
4. Detect the peaks according to the criteria described in Eq. (10) and compute the four statistics as described above. Thus the affine invariant texture features are derived.

4. Experimental results

In our experiments, we demonstrate the capability of the proposed features in affine invariant texture classification in Section 4.2. Then the efficacy of this method is tested in the context of affine invariant image retrieval in Section 4.3.

4.1. Image database

A test database is constructed for the experiments. The database consists of 20 structural texture images from the Brodatz texture album as shown in Fig. 5 (if textures are isotropic or random, any texture descriptors may be invariant to affine transforms, especially rotation [16]). Each texture image of size 512×512 is randomly affine transformed into 50 versions, from which subimages of size 128×128 are extracted. Thus a database of 1000 (50 for each texture class) images is constructed.

4.2. Affine invariant texture classification

The performance of the proposed features is first tested in affine invariant texture classification. One-hundred and forty images from the above database (seven for each texture class) are used for training and the remaining 860 images (43 for each texture) for testing. The PDV is extracted from each image and the feature vector is constructed by computing statistics of PDV as discussed in Section 3. Euclidean distance is calculated to measure the similarity between textures. Suppose that f_i represents the i th component of the feature vector f , $i = 1, 2, 3, 4$. The distance D between textures f and f' is calculated as follows:

$$D = \sqrt{\sum_{i=1}^4 (f_i - f'_i)^2}.$$

The K-nearest neighborhood classifier is employed. An average correct recognition rate of 87.91% is obtained. The classification confusion matrix in Table 1 shows the classification results of each texture. It is interesting to notice

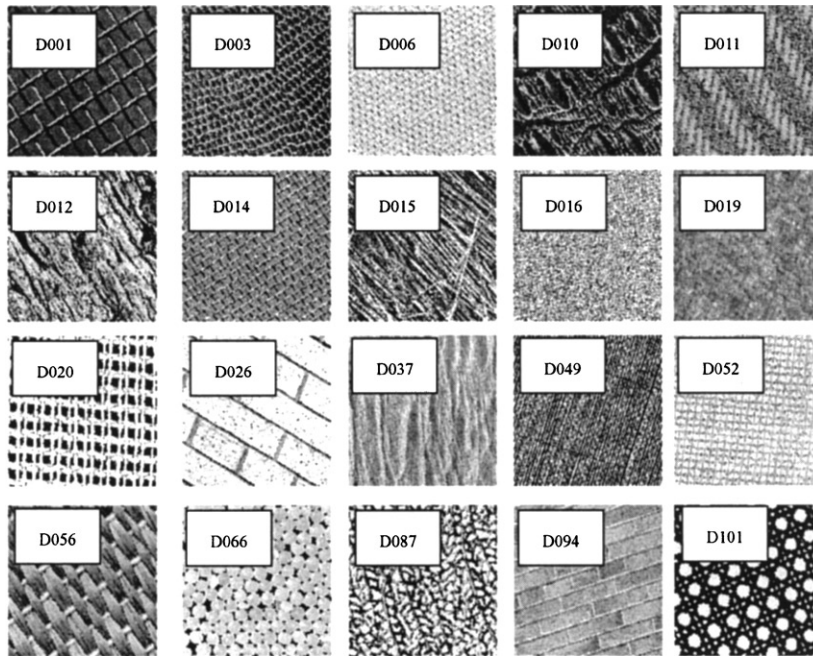


Fig. 5. Twenty textures from Brodatz database used for affine invariant texture classification.

Table 1
Confusion matrix of affine invariant texture classification

| Reference texture | No. of matches with | | | | | | | | | | | | | | | | | | | |
|-------------------|---------------------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|
| | D001 | D003 | D006 | D010 | D011 | D012 | D014 | D015 | D016 | D019 | D020 | D026 | D037 | D049 | D052 | D056 | D066 | D087 | D094 | D101 |
| D001 | 41 | | | 2 | | | | | | | | | | | | | | | | |
| D003 | | 38 | | | | | | | | | | | | 4 | | | | | | 1 |
| D006 | | | 43 | | | | | | | | | | | | | | | | | |
| D010 | 2 | | | 41 | | | | | | | | | | | | | | | | |
| D011 | | | | | 42 | | | | | | | | | | | 1 | | | | |
| D012 | | | | | | 35 | | | | 4 | | | | | | | | | | 4 |
| D014 | | | | | | | 37 | | 5 | | | | 1 | | | | | | | |
| D015 | | | 2 | | | | | 40 | | | | | | | | 1 | | | | |
| D016 | | | | | 1 | | 4 | | 18 | 14 | | | | | | 6 | | | | |
| D019 | | | | | | | | | 17 | 26 | | | | | | | | | | |
| D020 | | | | | | | | | | | 42 | | | | | | | | | 1 |
| D026 | | | 3 | | | | | | | | | 40 | | | | | | | | |
| D037 | | | | | | | 1 | | 1 | | | | 39 | | | | | | | |
| D049 | | 4 | | | | | | | | | | | | 39 | | | | | | |
| D052 | | | | | | | | | | | | | | | 40 | | | | | |
| D056 | | | | | 8 | | | 2 | | | | | 1 | | 32 | | | | | |
| D066 | | | | | | | | | | | | | | | 2 | 41 | | | | |
| D087 | | | | | | 2 | | | | | | | 1 | | | | 40 | | | |
| D094 | | | | | | | | | | | 4 | | | 1 | | | | | | 39 |
| D101 | | | | | | | | | | | | | | | | | | | | 43 |

Average accuracy = 87.91%

that major misclassifications occur between D016 and D019. The two textures are indeed the most similar ones in that both are more random than others.

4.3. Image retrieval

In this section, we further test the proposed texture features in the context of affine invariant image retrieval. It

should be pointed out that although much has been done on content-based image retrieval [1], little attention has been paid to affine invariant image retrieval despite of its scientific and practical value. We do this in an image retrieval system. A query texture is presented to the system. Fifty texture images are returned as the most similar images to the prototype per search. The retrieval database contains 1000 images described above.

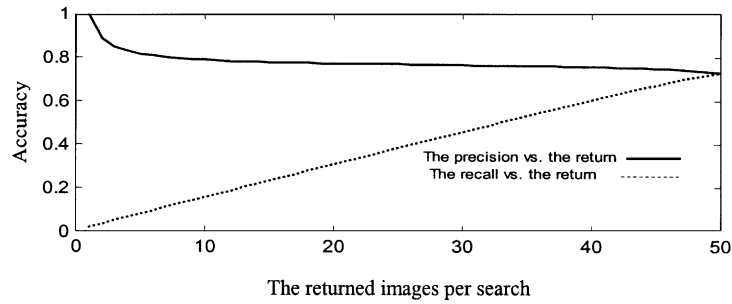


Fig. 6. Performance of affine invariant texture retrieval.

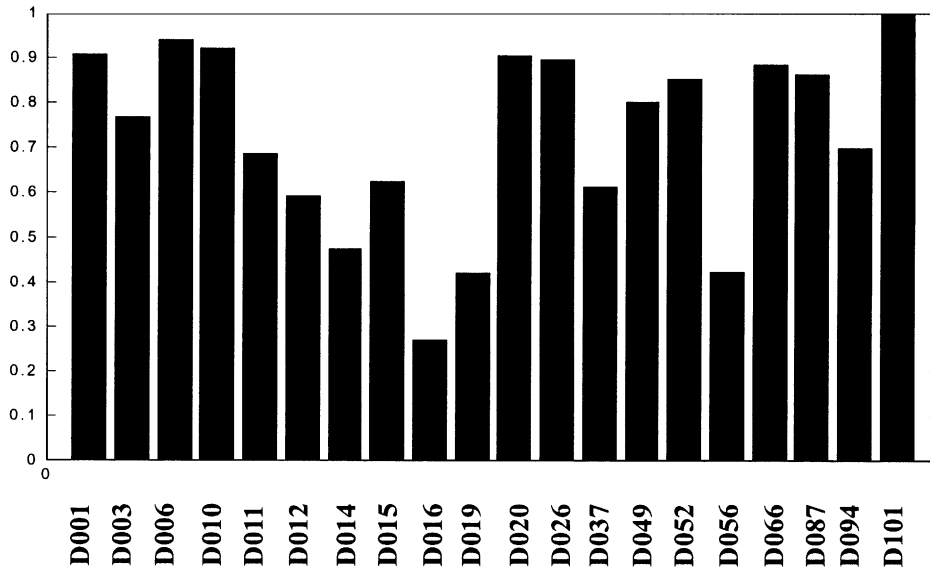


Fig. 7. Retrieval results of each texture class as 50 images returned per search.

In this experiment, the performance criterion is quantitative. The perfect retrieval results for a query texture should be an image subset whose elements are of the same class as the query image. The criterion lies on the fact that a texture image and its affine transformed versions are always perceived as the same textures by human observers. That is, they are viewpoint independent and perceptually similar.

The retrieval system is evaluated by the precision and recall measurement [1]. Suppose the image database is divided into two sets: the set of images $R(q)$ predetermined to be of the same class as the query q , and the set of irrelevant images. Assume that the query image q is presented to the retrieval system and the system returns a set of images $A(q)$ as the answer. The precision of the answer is the fraction of the returned images that are relevant to the query

$$p = \frac{A(q) \cap R(q)}{A(q)}$$

Whereas the recall is the fraction of relevant images that are returned by the query

$$r = \frac{A(q) \cap R(q)}{R(q)}$$

We explore the performance of our retrieval system by computing p and r via changing the number of the returned images per search. The evaluation results are illustrated in Fig. 6. An average of 38 out of 50 images returned is of the same texture class. The retrieval performance is shown in Fig. 6 as the number of returned images increases. We can see that the precision is robust to the returned images. The recall rate increases fast versus the number of the returned images (notice that the ideal recall should reach 100% when the number of returned images increases to 50). Fig. 6 illustrates that our method gives a very encouraging precision while keeping good recall rate. This clearly shows the efficacy of the proposed method for affine invariant texture

based retrieval. The retrieval result of each texture class is illustrated in Fig. 7. Experimental results in Fig. 7 and Table 1 show that a texture that gives good classification also gives good retrieval results.

5. Discussion and conclusions

It has been reported that Gabor features and Wold features can characterize both ordered and random textures [16,17]. To the best of our knowledge [7,8], these texture models have not been developed for affine invariant texture classification. The spectrum signatures described in this paper are comparable to these features in measuring texture periodicity. When Gabor masks are tuned to the orientations indicated by larger spectrum signatures, the Gabor channels often produce larger output. For Wold features, the harmonic peaks that can measure texture structural properties are often centered on those regions around the orientations indicated by the peaks in $T(\theta)$. This suggests that our features can capture texture properties as many other texture models do. Furthermore they are invariant to affine transforms.

In conclusion, we have presented a novel algorithm for extracting affine invariant texture features. Our experimental study has clearly shown the efficacy of the proposed features in both invariant texture classification and CBAIR. This is a good start in affine invariant texture analysis. This approach may be extended to perspective invariant texture classification.

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